## Photon induced processes from semi-central to ultraperipheral collisions: Introduction

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# Outline

#### Peripheral/ultraperipheral collisions

Weizsäcker-Williams fluxes of equivalent photons electromagnetic dissociation of heavy nuclei

#### "Soft to hard" in the diffractive photoproduction of vector mesons

diffractive dissociation color dipole approach  $J/\psi$  photoproduction on the proton

#### Diffractive processes on the nuclear target & multiple scattering expansion

Coherent exclusive & incoherent diffraction with breakup of nucleus production in ultraperipheral HI collisions

#### From ultraperipheral to semicentral collisions

dileptons from  $\gamma\gamma$  production vs thermal dileptons from plasma phase diffractive  $J/\psi$  in semi-central collisions

### 🔋 A. Łuszczak and W. S., Phys. Rev. C 97 (2018) no.2, 024903 [arXiv:1712.04502 [hep-ph]].

A. Łuszczak and W. S., arXiv:1901.07989 [hep-ph].

M. Kłusek-Gawenda, R. Rapp, W. S. and A. Szczurek, Phys. Lett. B **790** (2019) 339 [arXiv:1809.07049 [nucl-th]].

# Centrality



• e.g. from optical limit of Glauber:

$$rac{d\sigma_{
m AA}^{
m in}}{db} = 2\pi b (1-e^{-\sigma_{
m NN}^{
m in} T_{
m AA}(b)})$$

 $\sigma_{AA}^{in} \sim$  7 barn for Pb at LHC.

 $\bullet$  fraction of inelastic hadronic events contained in the centrality class  $\mathcal{C},$ 

$$f_{\mathcal{C}} = rac{1}{\sigma_{\mathrm{AA}}^{\mathrm{in}}} \int_{b_{\mathrm{min}}}^{b_{\mathrm{max}}} db rac{d\sigma_{\mathrm{AA}}^{\mathrm{in}}}{db} \, .$$

- experimentally, centrality is determined by binning in multiplicity and/or transverse energy.
- Probability of no inelastic interaction:

$$P_{\text{surv}}(\boldsymbol{b}) = \exp[-\sigma_{\text{NN}}^{\text{in}} T_{\text{AA}}(\boldsymbol{b})] \sim \theta(\boldsymbol{b} - 2R_{\text{A}})$$

### Fermi-Weizsäcker-Williams equivalent photons

Heavy nuclei Au, Pb have  $Z \sim 80$ 



- ion at rest: source of a Coulomb field, the highly boosted ion: sharp burst of field strength, with  $|\mathbf{E}|^2 \sim |\mathbf{B}|^2$  and  $\mathbf{E} \cdot \mathbf{B} \sim 0$ . (See e.g. J.D Jackson textbook).
- acts like a flux of "equivalent photons" (photons are collinear partons).

$$\boldsymbol{E}(\omega, \boldsymbol{b}) = -i \frac{Z\sqrt{4\pi\alpha_{em}}}{2\pi} \frac{\boldsymbol{b}}{b^2} \frac{\omega \boldsymbol{b}}{\gamma} \mathcal{K}_1\left(\frac{\omega \boldsymbol{b}}{\gamma}\right); \mathcal{N}(\omega, \boldsymbol{b}) = \frac{1}{\omega} \frac{1}{\pi} \left| \boldsymbol{E}(\omega, \boldsymbol{b}) \right|^2$$
$$\sigma(AB) = \int d\omega d^2 \boldsymbol{b} \, \mathcal{N}(\omega, \boldsymbol{b}) \, \sigma(\gamma B; \omega)$$

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### Finite size of particle $\rightarrow$ charge form factor



- Seen from a large distance, the ion indeed acts like a pointlike charge.
- When we come closer, the finite-size charge distribution important. Sometimes its effect is simulated by a sharp lower cutoff in *b*.

# **Ultraperipheral collisions**

some examples of ultraperipheral processes:



- photoabsorption on a nucleus
- diffractive photoproduction with and without breakup/excitation of a nucleus
- $\gamma\gamma$ -fusion.
- electromagnetic excitation/dissociation of nuclei. Excitation of Giant Dipole Resonances.
- the intact nuclei in the final state are not measured. Each of the photon exchanges is associated with a large rapidity gap.
- very small  $p_T$  of the photoproduced system.

### Absorption corrected flux of photons



• survival probability:

$$P_{\text{surv}}(\boldsymbol{b}) = S_{el}^2(\boldsymbol{b}) = \exp\left(-\sigma_{NN}T_{A_1A_2}(\boldsymbol{b})\right) \sim \theta(|\boldsymbol{b}| - (R_1 + R_2))$$

### Electromagnetic excitation of heavy ions



• Huge peak in the photoabsorption cross section - Giant Dipole Resonance.

### Electromagnetic excitation of heavy ions



- Giant dipole resonance decays through emission of few neutrons.
- experimental data on excitation functions for the reactions  $\gamma^{208}Pb \rightarrow k \text{ neutrons} + Pb$  allow us to calculate the fractions f(E, k) of a final state with k = 1, 2, 3 neutrons.
- we can calculate "topological cross sections" with given numbers of neutrons in the forward region of either ion.
- Monte Carlo Code "Gemini" for evaporation of neutrons based on Hauser-Feshbach Theory.

$$\sigma(A_1A_2 \to (m\mathrm{N}, X)(k\mathrm{N}, Y)) = \int d^2 \boldsymbol{b} \, P_{\mathrm{surv}}(\boldsymbol{b}) \, P_{A_1}^{\mathrm{exc}}(\boldsymbol{b}, m) \, P_{A_2}^{\mathrm{exc}}(\boldsymbol{b}, k) \, .$$

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## Electromagnetic excitation of heavy ions



- electromagnetic dissociation cross section for <sup>208</sup>Pb. Data from SPS and LHC (ALICE).
- calculations from M. Kłusek-Gawenda, M. Ciemala, W. S. and A. Szczurek, Phys. Rev. C 89 (2014) 054907.
- $\bullet\,$  cross section at LHC  $\sim 200\,$  barn!
- these processes play an important role as "triggers" for ultraperipheral processes.

## Inelastic diffraction: kinematics & t-channel exchanges



- To bridge a gap (say Δy ≥ 3) : α(0) ≥ 1 (Pomeron, C= +1; Odderon(??), C = -1).
- Exchange of secondary Reggeons:  $\alpha(0)=0.5$  for  $\rho,\omega,f2,a1$ ;  $\alpha(0)=0$  for pions dies out exponentially with the gap size (no exchange of color or charge over a large gap!).
- Pomeron/Odderon: multigluon exchanges; Reggeons: q q exchange
- Photons (J=1, C=-1) also qualify!

# **Total photoproduction cross sections**



- From soft to hard diffraction in the photoproduction of vector mesons.
- Pomeron intercept depends on the meson...

# **Vector Meson Dominance**



Extrapolate from the VM-pole to spacelike region:

$$A(\gamma^*(Q^2)p \rightarrow Vp; W, t) = \sqrt{rac{3\Gamma(V^0 \rightarrow e^+e^-)}{M_V lpha_{em}}} \, rac{M_V^2}{Q^2 + M_V^2} \, A(Vp \rightarrow Vp; W, t)$$

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### **Vector Meson Dominance**

Extrapolate from the VM-pole to spacelike region:

$$A(\gamma^*(Q^2)p o Vp; W, t) = \sqrt{rac{3\Gamma(V^0 o e^+e^-)}{M_V lpha_{em}}} \, rac{M_V^2}{Q^2 + M_V^2} \, A(Vp o Vp; W, t)$$

- hadronic structure of the photon
- parameters of  $A(Vp \rightarrow Vp; W, t)$  can be taken from  $\pi N$  elastic scattering

$$\Im mA(Vp \to Vp; W, t = 0) = s \cdot \sigma_{\text{tot}}(Vp)$$
  
$$\sigma_{\text{tot}}(\rho^0 p) = \sigma_{\text{tot}}(\omega p) = \frac{1}{2}(\sigma_{\text{tot}}(\pi^+ p) + \sigma_{\text{tot}}(\pi^- p))$$
  
$$\sigma_{\text{tot}}(\phi p) = \sigma_{\text{tot}}(K^+ p) + \sigma_{\text{tot}}(K^- n) - \sigma_{\text{tot}}(\pi^+ p)$$

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- works well for photoproduction of  $\rho, \omega$ ,
- cannot be correct in the deeply spacelike region  $Q^2 \gg M_V^2$
- connection to QCD degrees of freedom at large  $Q^2$  ?
- heavy flavours ?

# Color dipole/ $k_{\perp}$ -factorization approach



Color dipole representation of forward amplitude:

$$d(\gamma^*(Q^2)p \to Vp; W, t = 0) = \int_0^1 dz \int d^2 r \,\psi_V(z, r) \,\psi_{\gamma^*}(z, r, Q^2) \,\sigma(x, r)$$
  
 $\sigma(x, r) = \frac{4\pi}{3} \alpha_S \int \frac{d^2 \kappa}{\kappa^4} \frac{\partial G(x, \kappa^2)}{\partial \log(\kappa^2)} \left[1 - e^{i\kappa r}\right], \, x = M_V^2/W^2$ 

• impact parameters and helicities of high-energy q and  $\bar{q}$  are conserved during the interaction.

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 scattering matrix is "diagonal" in the color dipole representation. Color dipoles as "Good-Walker states".

### When do small dipoles dominate ?

• the photon shrinks with  $Q^2$  - photon wavefunction at large r:

$$\psi_{\gamma^*}(\boldsymbol{z}, \boldsymbol{r}, Q^2) \propto \exp[-\varepsilon r], \, \varepsilon = \sqrt{m_f^2 + z(1-z)Q^2}$$

• the integrand receives its main contribution from

$$r \sim r_S pprox rac{6}{\sqrt{Q^2 + M_V^2}}$$

Kopeliovich, Nikolaev, Zakharov '93

- ullet a large quark mass (bottom, charm) can be a hard scale even at  $Q^2 
  ightarrow 0.$
- for small dipoles we can approximate

$$\sigma(x,r) = \frac{\pi^2}{3} r^2 \alpha_5(q^2) x g(x,q^2), \ q^2 \approx \frac{10}{r^2}$$

• for  $arepsilon \gg 1$  we then obtain the asymptotics

$$A(\gamma^* p \rightarrow V p) \propto r_S^2 \sigma(x, r_S) \propto rac{1}{Q^2 + M_V^2} imes rac{1}{Q^2 + M_V^2} xg(x, Q^2 + M_V^2)$$

probes the gluon distribution, which drives the energy dependence.

• From DGLAP fits:  $xg(x,\mu^2) = (1/x)^{\lambda(\mu^2)}$  with  $\lambda(\mu^2) \sim 0.1 \div 0.4$  for  $\mu^2 = 1 \div 10^2 \text{GeV}^2$ .

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Overlap of light-cone wave functions

$$\begin{split} \Psi_V^*(z,r)\Psi_\gamma(z,r) &= \frac{e_Q\sqrt{4\pi\alpha_{\rm em}}N_c}{4\pi^2 z(1-z)} \bigg\{ m_Q^2 K_0(m_Q r)\psi(z,r) \\ &- [z^2+(1-z)^2]m_Q K_1(m_Q r)\frac{\partial\psi(z,r)}{\partial r} \bigg\}. \end{split}$$

• "boosted Gaussian" wave functions as in Nemchik et al. ('94)

$$\psi(z,r)\propto z(1-z)\exp\left[-rac{M_Q^2R^2}{8z(1-z)}-rac{2z(1-z)r^2}{R^2}
ight]$$

• parameters  $m_Q, R$  & normalization as in Kowalski et al. (2006) for  $J/\psi$  and Cox et al. (2008) for  $\Upsilon$ .

#### diffractive slope on a free nucleon:

$$B = B_0 + 4\alpha' \log(W/W_0)$$
 with  $W_0 = 90 \text{ GeV}$ , and  $\alpha' = 0.164 \text{ GeV}^{-2}$   
We take  $B_0 = 4.88 \text{ GeV}^{-2}$  for  $J/\psi$  and  $B_0 = 3.68 \text{ GeV}^{-2}$  for  $\Upsilon$ .

BGK-form of the dipole cross section

$$\sigma(x,r) = \sigma_0 \left( 1 - \exp\left[ -\frac{\pi^2 r^2 \alpha_s(\mu^2) x g(x,\mu^2)}{3\sigma_0} \right] \right), \mu^2 = C/r^2 + \mu_0^2$$

• the soft ansatz, as used in the original BGK model

$$xg(x,\mu_0^2) = A_g x^{-\lambda_g} (1-x)^{C_g},$$

• the soft + hard ansatz

$$xg(x, \mu_0^2) = A_g x^{-\lambda_g} (1-x)^{C_g} (1+D_g x+E_g x^2),$$

- fit I: BGK fit with fitted valence quarks for  $\sigma_r$  for H1ZEUS-NC data in the range  $Q^2 \ge 3.5 \text{ GeV}^2$  and  $x \le 0.01$ . NLO fit. Soft gluon.
- fit II: BGK fit with valence quarks for  $\sigma_r$  for H1ZEUS-NC data in the range  $Q^2 \ge 0.35$  GeV<sup>2</sup> and  $x \le 0.01$ . NLO fit. Soft + hard gluon.
- fits from A. Łuszczak and H. Kowalski, Phys. Rev. D 95 (2017).

#### numerically important corrections:

• real part of the diffractive amplitude:

$$\sigma(x,r) o (1-i
ho(x))\sigma(x,r)\,,\,
ho(x) = an\left(rac{\pi\Delta_{\mathbf{P}}}{2}
ight), \Delta_{\mathbf{P}} = rac{\partial\log\left(\langle V|\sigma(x,r)|\gamma
ight)}{\partial\log(1/x)}$$

 amplitude is non-forward also in the longitudinal momenta. Correction factor (Shuvaev et al. (1999)):

$$\mathsf{R}_{\mathrm{skewed}} = rac{2^{2\Delta_{\mathbf{P}}+3}}{\sqrt{\pi}} \cdot rac{\Gamma(\Delta_{\mathbf{P}}+5/2)}{\Gamma(\Delta_{\mathbf{P}}+4)}$$

apply K-factor to the cross section:

$$K = (1 + \rho^2(x)) \cdot R_{\text{skewed}}^2.$$

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- besides the BGK-fit of Łuszczak & Kowalski, we show to other dipole cross section fits which incorporate heavy quarks:
  - (1) 'IIM' (lancu, Itakura & Munier, which is a parametrization inspired by BFKL/BK-asymptotics).
  - a recent re-fit of the Golec-Biernat-Wüsthoff form of the dipole cross section obtained by Golec-Biernat & Sapeta (2018).
- the data at high energies were in fact extracted from exclusive diffraction in pp-collisions by LHCb.
- $\bullet\,$  note: for our applications on nuclear targets, the region of  $W\sim30\div100\,{\rm GeV}$  is the most relevant.

### Diffractive processes on the nuclear target



#### diffractive processes on nuclear targets:

- coherent diffraction nucleus stays in the ground state
- complete breakup of the nucleus, final state free protons & neutrons
- intact nucleus, but an excited state
- partial breakup of the nucleus, a variety of possible fragments

#### they all have in common:

- large rapidity gap between vector meson and nuclear fragments
- lack of production of additional particles

# **Off-forward amplitude**

Amplitude at finite transverse momentum transfer  $\Delta$ 

$$\mathcal{A}(\gamma^* A_i \to V A_f^*; W, \Delta) = 2i \int d^2 \boldsymbol{B} \exp[-i\boldsymbol{\Delta} \boldsymbol{B}] \langle V|\langle A_f^*|\hat{\Gamma}(\boldsymbol{b}_+, \boldsymbol{b}_-)|A_i\rangle|\gamma\rangle$$
$$= 2i \int d^2 \boldsymbol{B} \exp[-i\boldsymbol{\Delta} \boldsymbol{B}] \int_0^1 dz \int d^2 \boldsymbol{r} \Psi_V^*(z, \boldsymbol{r}) \Psi_\gamma(z, \boldsymbol{r}) \langle A_f^*|\hat{\Gamma}(\boldsymbol{B} - (1-z)\boldsymbol{r}, \boldsymbol{B} + z\boldsymbol{r})|A_i\rangle.$$

$$r = b_{+} - b_{-}, \ b = (b_{+} + b_{-})/2,$$
  
$$B = zb_{+} + (1 - z)b_{-} = b - (1 - 2z)\frac{r}{2}$$



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# **Coherent diffraction – Glauber averages**

$$\mathcal{A}(\gamma^* A_i \to V A_i; W, \Delta) = 2i \int d^2 \boldsymbol{b} \exp[-i\boldsymbol{b}\boldsymbol{\Delta}] \int d^2 \boldsymbol{r} \rho_{V\gamma}(\boldsymbol{r}, \boldsymbol{\Delta}) \langle A_i | \hat{\Gamma}(\boldsymbol{b} + \frac{\boldsymbol{r}}{2}, \boldsymbol{b} - \frac{\boldsymbol{r}}{2}) | A_i \rangle,$$
  
$$\rho_{V\gamma}(\boldsymbol{r}, \boldsymbol{\Delta}) = \int_0^1 dz \exp[i(1-2z)\frac{\boldsymbol{r}\boldsymbol{\Delta}}{2}] \Psi_V^*(z, \boldsymbol{r}) \Psi_\gamma(z, \boldsymbol{r}).$$

$$\hat{\Gamma}(\boldsymbol{b}_{+}, \boldsymbol{b}_{-}) = 1 - \prod_{i=1}^{A} [1 - \hat{\Gamma}_{N_{i}}(\boldsymbol{b}_{+} - \boldsymbol{c}_{i}, \boldsymbol{b}_{-} - \boldsymbol{c}_{i})],$$

in the limit of the dilute uncorrelated nucleus all we need are:

$$M(\boldsymbol{b}_+, \boldsymbol{b}_-) = \int d^2 \boldsymbol{c} T_A(\boldsymbol{c}) \Gamma_N(\boldsymbol{b}_+ - \boldsymbol{c}, \boldsymbol{b}_- - \boldsymbol{c}) \approx \frac{1}{2} \sigma(\boldsymbol{r}) T_A(\boldsymbol{b})$$

$$\langle A_i | \hat{\Gamma}(\boldsymbol{b} + \frac{\boldsymbol{r}}{2}, \boldsymbol{b} - \frac{\boldsymbol{r}}{2}) | A_i \rangle = 1 - \left[ 1 - \frac{1}{A} M(\boldsymbol{b}_+, \boldsymbol{b}_-) \right]^A \approx 1 - \exp[-\frac{1}{2} \sigma(\boldsymbol{r}) T_A(\boldsymbol{b})]$$

# Incoherent diffraction: summing over nuclear states

$$\frac{d\sigma_{\rm incoh}}{d\mathbf{\Delta}^2} = \sum_{A_f \neq A} \frac{d\sigma(\gamma A_i \to V A_f^*)}{d\mathbf{\Delta}^2}$$

Closure in the sum over nuclear final states:

$$\sum_{A
eq A_f} |A_f
angle \langle A_f| = 1 - |A
angle \langle A|,$$

$$rac{d\sigma_{
m incoh}}{d\mathbf{\Delta}^2} = rac{1}{4\pi} \int d^2 \mathbf{r} d^2 \mathbf{r}' 
ho_{V\gamma}^*(\mathbf{r}',\mathbf{\Delta}) 
ho_{V\gamma}(\mathbf{r},\mathbf{\Delta}) \Sigma_{
m incoh}(\mathbf{r},\mathbf{r}',\mathbf{\Delta})\,,$$

$$\Sigma_{\rm incoh}(\mathbf{r},\mathbf{r}',\mathbf{\Delta}) = \int d^2 \mathbf{b} d^2 \mathbf{b}' \exp[-i\mathbf{\Delta}(\mathbf{b}-\mathbf{b}')] \mathcal{C}\left(\mathbf{b}'+\frac{\mathbf{r}'}{2},\mathbf{b}'-\frac{\mathbf{r}'}{2};\mathbf{b}+\frac{\mathbf{r}}{2},\mathbf{b}-\frac{\mathbf{r}}{2}\right)$$

Only ground state nuclear averages:

$$\mathcal{C}(\boldsymbol{b}'_+,\boldsymbol{b}'_-;\boldsymbol{b}_+,\boldsymbol{b}_-) = \langle A|\hat{\Gamma}^{\dagger}(\boldsymbol{b}'_+,\boldsymbol{b}'_-)\hat{\Gamma}(\boldsymbol{b}_+,\boldsymbol{b}_-)|A\rangle - \langle A|\hat{\Gamma}(\boldsymbol{b}'_+,\boldsymbol{b}'_-)|A\rangle^* \langle A|\hat{\Gamma}(\boldsymbol{b}_+,\boldsymbol{b}_-)|A\rangle \,.$$

# Nuclear averages as in Glauber & Matthiae

$$\hat{\Gamma}(\boldsymbol{b}_+, \boldsymbol{b}_-) = 1 - \prod_{i=1}^A [1 - \hat{\Gamma}_{N_i}(\boldsymbol{b}_+ - \boldsymbol{c}_i, \boldsymbol{b}_- - \boldsymbol{c}_i)],$$

in the limit of the dilute uncorrelated nucleus all we need are:

$$M(b_{+}, b_{-}) = \int d^{2}c T_{A}(c) \Gamma_{N}(b_{+} - c, b_{-} - c)$$
  

$$\Omega(b'_{+}, b'_{-}; b_{+}, b_{-}) = \int d^{2}c T_{A}(c) \Gamma_{N}^{*}(b'_{+} - c, b'_{-} - c) \Gamma_{N}(b_{+} - c, b_{-} - c)$$

$$C(\mathbf{b}'_{+}, \mathbf{b}'_{-}; \mathbf{b}_{+}, \mathbf{b}_{-}) = \left[1 - \frac{1}{A} \left(M^{*}(\mathbf{b}'_{+}, \mathbf{b}'_{-}) + M(\mathbf{b}_{+}, \mathbf{b}_{-})\right) + \frac{1}{A} \Omega(\mathbf{b}'_{+}, \mathbf{b}'_{-}; \mathbf{b}_{+}, \mathbf{b}_{-})\right]^{A} - \left[\left(1 - \frac{1}{A}M^{*}(\mathbf{b}'_{+}, \mathbf{b}'_{-})\right) \left(1 - \frac{1}{A}M(\mathbf{b}_{+}, \mathbf{b}_{-})\right)\right]^{A}$$

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# Multiple scattering expansion of the incoherent cross section

Diffraction cone of the free nucleon:  $B \ll R_A^2$ 

$$\sigma(x, \mathbf{r}, \mathbf{\Delta}) = \sigma(x, \mathbf{r}) \exp[-\frac{1}{2}B\mathbf{\Delta}^2]$$

Multiple scattering expansion for  $\Delta^2 R_A^2 \gg 1$ 

$$\frac{d\sigma_{\rm incoh}}{d\mathbf{\Delta}^2} = \sum_n \frac{d\sigma^{(n)}}{d\mathbf{\Delta}^2} = \frac{1}{16\pi} \sum_n w_n(\mathbf{\Delta}) \int d^2 \boldsymbol{b} T_A^n(\boldsymbol{b}) |I_n(\boldsymbol{x}, \boldsymbol{b})|^2,$$

$$w_n(\mathbf{\Delta}) = \frac{1}{n \cdot n!} \cdot \left(\frac{1}{16\pi B}\right)^{n-1} \cdot \exp\left(-\frac{B}{n}\mathbf{\Delta}^2\right),$$

and

$$I_n(x, \mathbf{b}) = \langle V | \sigma^n(x, r) \exp[-\frac{1}{2}\sigma(x, r)T_A(\mathbf{b})] | \gamma \rangle$$
  
= 
$$\int_0^1 dz \int d^2 \mathbf{r} \Psi_V^*(z, \mathbf{r}) \Psi_\gamma(z, \mathbf{r}) \sigma^n(x, r) \exp[-\frac{1}{2}\sigma(x, r)T_A(\mathbf{b})] \cdot \prod_{\text{nuclear absorption}} \cdot \prod_{\text{nuclear absorpti}} \cdot \prod_{\text{nuclear absorption}} \cdot \prod_{\text{nuclear$$



 $-t={\bf \Delta}^2~$  , single scattering has the same diffractive slope as on the free nucleon, multiple scatterings have smaller slopes.

at low  $\pmb{\Delta}^2$  the single scattering dominates, and one should rather use its exact form:

$$\frac{d\sigma_{\text{incoh}}}{d\mathbf{\Delta}^2} = \frac{1}{16\pi} \left\{ w_1(\mathbf{\Delta}) \int d^2 \boldsymbol{b} T_A(\boldsymbol{b}) |l_1(x, \boldsymbol{b})|^2 - \underbrace{\frac{1}{A} \left| \int d^2 \boldsymbol{b} \exp[-i\mathbf{\Delta}\boldsymbol{b}] T_A(\boldsymbol{b}) l_1(x, \boldsymbol{b}) \right|^2}_{\text{vanishes for } \mathbf{\Delta}^2 \mathrm{R}^2_A \gg 1} \right\}.$$

$$I_1(x, \boldsymbol{b}) = \langle V | \sigma(x, r) \underbrace{\exp[-\frac{1}{2}\sigma(x, r)T_A(\boldsymbol{b})]}_{\text{nuclear absorption}} | \gamma$$

If we were to neglect intranuclear absorption, we would obtain for small  $\pmb{\Delta}^2$ :

$$\frac{d\sigma_{\rm incoh}}{d\mathbf{\Delta}^2} = A \cdot \frac{d\sigma(\gamma N \to V N)}{d\mathbf{\Delta}^2} \Big|_{\mathbf{\Delta}^2=0} \cdot \left\{ 1 - \mathcal{F}_A^2(\mathbf{\Delta}^2) \right\}.$$

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### Diffractive processes on the nuclear target



- solid line: exact single scattering
- dashed: large |t|-limit of single scattering
- exact result merges into the large |t| limit quickly, the latter is a good approximation in a broad range of t.
- cross section dips, but does not vanish at  $t \rightarrow 0$ .
- note: in the small to intermediate *t* region nuclear correlations may play a role.

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## Diffractive processes on the nuclear target



- blue:  $\Upsilon$ , red:  $J/\psi$
- dashed line: dipole fit I (soft gluon),
- solid line: dipole fit II (soft+hard gluon)
- dependence on dipole cross section in its "applicability region" is rather small.
- nuclear absorption cannot be neglected, even for heavy vector mesons.

$$R_{\rm incoh}(x) = \frac{d\sigma_{\rm incoh}/d\mathbf{\Delta}^2}{A \cdot d\sigma(\gamma N \to VN)/d\mathbf{\Delta}^2} = \frac{\int d^2 \boldsymbol{b} T_A(\boldsymbol{b}) \left| \langle V | \sigma(x,r) \exp[-\frac{1}{2}\sigma(x,r)T_A(\boldsymbol{b})] | \gamma \rangle \right|^2}{A \cdot \left| \langle V | \sigma(x,r) | \gamma \rangle \right|^2}.$$



solid line: with skewedness/real part correction dashed line: without corr. data point from ALICE Eur. Phys. J. C **73** (2013)

Cross section for AA collision uses Weizsäcker-Williams photon fluxes:

$$rac{d\sigma_{
m incoh}(AA 
ightarrow VAX)}{dy} = n_{\gamma/A}(z_+)\sigma_{
m incoh}(W_+) + n_{\gamma/A}(z_-)\sigma_{
m incoh}(W_-)\,,$$

$$z_{\pm} = rac{m_V}{\sqrt{s_{NN}}} e^{\pm y}, \ W_{\pm} = \sqrt{z_{\pm}s_{NN}} \,.$$

# Coherent photoproduction of $J/\psi$ in heavy ion collisions



- $p_1, p_2 =$  transverse momenta of outgoing ions.
- Interference induces azimuthal correlation  $(\mathbf{p}_1 \cdot \mathbf{p}_2)/(t_1 t_2)$ .
- the interference is concentrated at very low  $p_T$  of  $J/\psi$  and can be neglected in rapidity distributions.

# Energies available for photoproduction

$\sqrt{s_{NN}} = 2.76 \mathrm{TeV}$						
у	$W_+[GeV]$	$W_{-}[GeV]$	x+	x_	$n(\omega_+)$	$n(\omega_{-})$
0.0	92.5	92.5	$1.12 \cdot 10^{-3}$	$1.12 \cdot 10^{-3}$	69.4	69.4
1.0	152	56.1	$4.13 \cdot 10^{-4}$	$3.05 \cdot 10^{-3}$	39.5	100
2.0	251	34.0	$1.52 \cdot 10^{-4}$	$8.29 \cdot 10^{-3}$	14.5	132
3.0	414	20.6	$5.59 \cdot 10^{-5}$	$2.25 \cdot 10^{-2}$	1.68	163
3.8	618	13.8	$2.51 \cdot 10^{-5}$	$5.02 \cdot 10^{-2}$	0.03	188

Table: Subenergies  $W_{\pm}$  and Bjorken-x values  $x_{\pm}$  for  $\sqrt{s_{NN}} = 2.76 \text{ TeV}$  for a given rapidity y. Also shown are photon fluxes  $n(\omega_{\pm})$ .

$\sqrt{s_{NN}} = 5.02 \mathrm{TeV}$						
у	$W_+$ [GeV]	$W_{-}[GeV]$	x+	x_	$n(\omega_+)$	$n(\omega_{-})$
0.0	125	125	$6.17 \cdot 10^{-4}$	$6.17 \cdot 10^{-4}$	87.9	87.9
1.0	206	75.6	$2.27 \cdot 10^{-4}$	$1.68 \cdot 10^{-3}$	57.2	119
2.0	339	45.9	$8.35 \cdot 10^{-5}$	$4.56 \cdot 10^{-3}$	28.5	150
3.0	559	27.8	$3.07 \cdot 10^{-5}$	$1.24 \cdot 10^{-2}$	7.5	181
4.0	921	16.9	$1.13 \cdot 10^{-5}$	$3.37 \cdot 10^{-2}$	0.35	213
4.8	1370	11.3	$5.08 \cdot 10^{-6}$	$7.50 \cdot 10^{-2}$	0.001	238

**Table:** Subenergies  $W_{\pm}$  and Bjorken-*x* values  $x_{\pm}$  for  $\sqrt{s_{NN}} = 5.02 \text{ TeV}$  for a given rapidity *y*.



- reasonable description of experimental data.
- the highest  $\gamma N$  energy at y = 0, about  $W = 100 \,\text{GeV}$ .
- explicit higher Fock states,  $c\bar{c}g, c\bar{c}gg...?$



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• Preliminary data from ALICE & LHCb.

## Dilepton production in semi-central collisions



- Dileptons are a "classic" probe of the QGP.
- medium modifications of ρ, thermal dileptons
- dileptons from  $\gamma\gamma$  fusion have peak at very low pair transverse momentum.

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• can they be visible even in semi-central collisions?

### Dilepton production in semi-central collisions



$$rac{d\sigma_{II}}{d\xi d^2 oldsymbol{b}} = \int d^2 oldsymbol{b}_1 d^2 oldsymbol{b}_2 \, \delta^{(2)} (oldsymbol{b} - oldsymbol{b}_1 - oldsymbol{b}_2) {\sf N}(\omega_1, b_1) {\sf N}(\omega_2, b_2) rac{d\sigma(\gamma\gamma 
ightarrow l^+ l^-; \hat{f s})}{d(-\hat{t})} \; ,$$

where the phase space element is  $d\xi = dy_+ dy_- dp_t^2$  with  $y_{\pm}$ ,  $p_t$  and  $m_l$  the single-lepton rapidities, transverse momentum and mass, respectively, and

$$\omega_1 = rac{\sqrt{
ho_t^2 + m_l^2}}{2} \left( e^{y_+} + e^{y_-} 
ight) \,, \; \omega_2 = rac{\sqrt{
ho_t^2 + m_l^2}}{2} \left( e^{-y_+} + e^{-y_-} 
ight) \,, \; \hat{s} = 4 \omega_1 \omega_2 \;.$$

• we adopt the impact parameter definition of centrality, of course...

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$$\frac{dN_{II}[\mathcal{C}]}{dM} = \frac{1}{f_{\mathcal{C}} \cdot \sigma_{AA}^{in}} \int_{b_{\min}}^{b_{\max}} db \int d\xi \, \delta(M - 2\sqrt{\omega_1 \omega_2}) \frac{d\sigma_{II}}{d\xi db} \Big|_{\text{cuts}},$$

## Dilepton production: impact parameter distribution



- semi-central collisions are situated on the left side of the distribution, below b < 15 fm.
- starting from RHIC energies, the contribution from coherent photons is practically energy-independent.
- also notice the long tails of the ultraperipheral part. Their importance rises with energy.

# Dilepton production in semi-central collisions



- M. Kłusek-Gawenda, R. Rapp, W.S. & A. Szczurek, Phys.Lett. B790 (2019)
- electron pair  $P_T < 150$  MeV: dileptons from coherent photons dominate over a large range of centralities.

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• other mechanisms: medium modified  $\rho$ , thermal dileptons, Dalitz-decays ("cocktail").

### From ultraperipheral to peripheral nuclear collisions

Recently, the ALICE collaboration has observed a large enhancement of  $J/\psi$  mesons carrying very small  $p_T < 300 \text{ MeV}$  in the centrality classes corresponding to peripheral collisions.

**Centrality class**  $70 \div 90\%$ :

 $13\,{
m fm} < b < 15\,{
m fm}$ , photon fluxes by Contreras Phys. Rev. C 96 (2017)

$$egin{array}{rll} rac{d\sigma_{
m incoh}(AA o VX|70 \div 90\%)}{dy} &=& n_{\gamma/A}(z_+|70 \div 90\%)\sigma_{
m incoh}(W_+|p_T < p_T^{
m cut}) \ &+& n_{\gamma/A}(z_-|70 \div 90\%)\sigma_{
m incoh}(W_-|p_T < p_T^{
m cut}) \ &pprox 15\,\mu{
m b}\,, \end{array}$$

The ALICE measurement is [Phys. Rev. Lett. 116 (2016)]:

$$rac{d\sigma(AA o VX|70 \div 90\%; 2.5 < |y| < 4.0)}{dy} = 59 \pm 11 \pm 8\,\mu{
m b}\,.$$

For an estimate of the coherent contribution, see: M. Kłusek-Gawenda and A. Szczurek, Phys. Rev. C **93** (2016), See talk by Antoni Szczurek on Friday.

- $\bullet\,$  Even when nuclei don't touch each other, they have very large inelastic cross sections. EM dissociation  $\sim$  200 barn at LHC.
- Ultraperipheral heavy ion collisions give access to a lot of interesting processes. Photoproduction of  $J/\psi$  tells us about interaction of small dipoles with nuclear medium, potentially about the nuclear gluon distribution.
- Certain properties/phenomena can even carry over into the semi-central domain. Their exploration has just begun.

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