

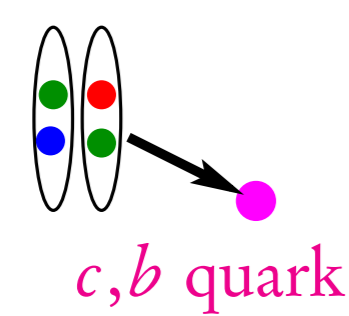
# Langevin approach to heavy-quark diffusion and quarkonium formation in the QGP

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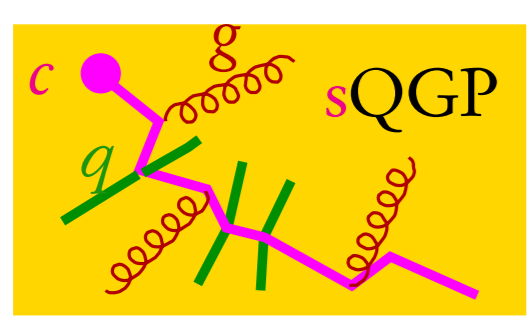
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## Introduction

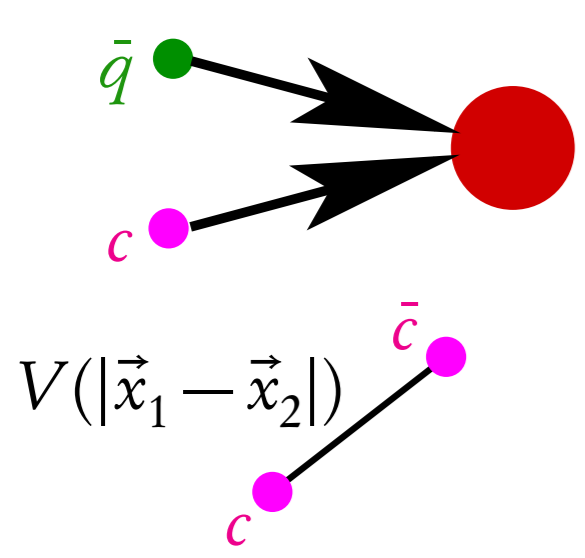
- **Strongly coupled** quark-gluon plasma (QGP)
  - ultrarelativistic heavy-ion collisions: medium well described by **hydrodynamics**
  - collective **radial and elliptic flow** ( $v_2$ ); constituent-quark number scaling of  $v_2$
  - low-viscosity **strongly coupled quark-gluon plasma**
- heavy-quark probes
  - heavy charm and bottom quarks produced in **primordial hard collisions**
  - calibrated initial conditions from pp collisions
  - conserved in **strong interactions** with bulk medium of light quarks and gluons
  - $R_{AA}$  and  $v_2$  of **D, B mesons** and **non-photonic single electrons**  $\leftrightarrow$  **transport properties** of the sQGP
  - can be described in **relativistic Fokker-Planck/Langevin model**
- theory scheme for heavy quarks



initial collisions: UrQMD + (3+1) hydro; Glauber model  
hard production of HQs  
described by PDF's + pQCD (PYTHIA)



HQ rescattering in QGP: **Langevin simulation**  
drag and diffusion coefficients from  
microscopic model for HQ interactions in the sQGP  
description of bulk matter: UrQMD + (3+1)-dim hydro



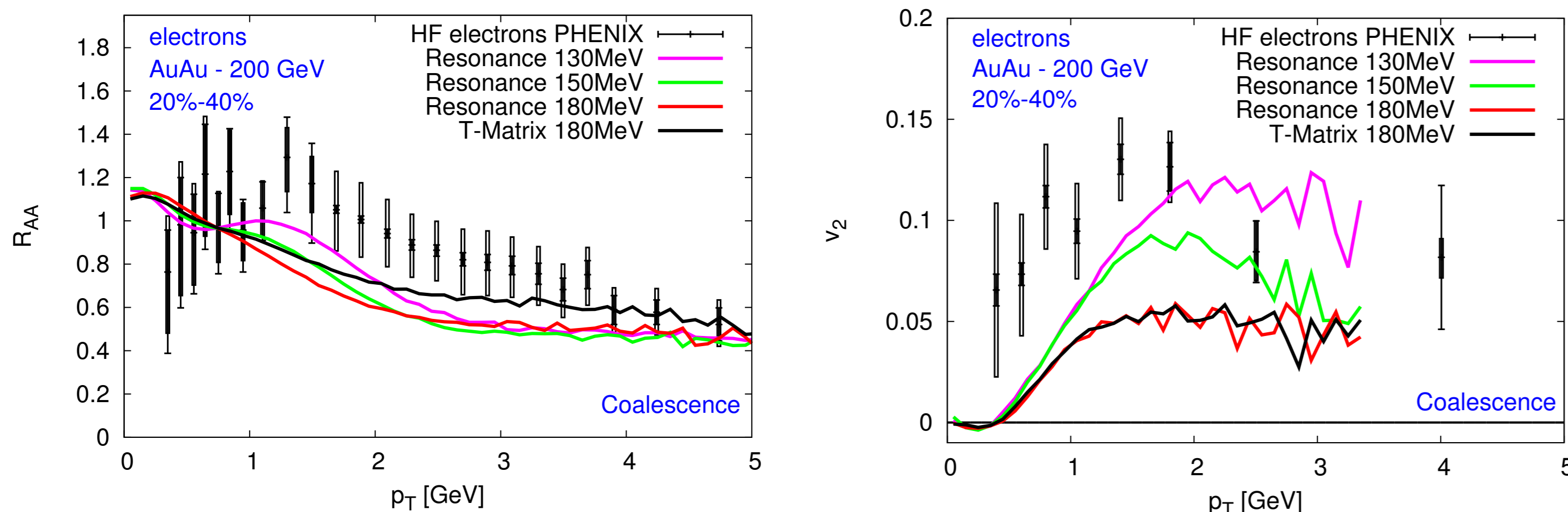
Hadronization to **D, B mesons** via  
**quark coalescence + fragmentation**

$c\bar{c}$ -pair can form (classical) bound state  $\leftrightarrow$  quarkonia

## Heavy-quark diffusion

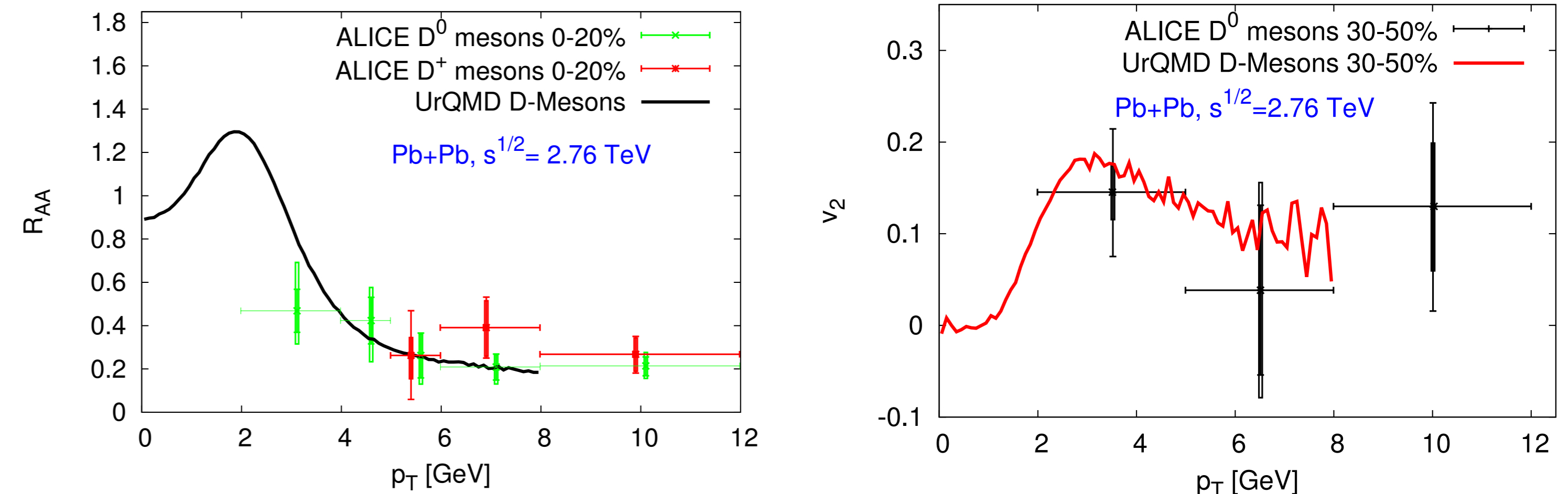
- Relativistic Langevin simulation
  - **heavy-quark diffusion** in hydrodynamic background
$$d\vec{x} = \frac{\vec{p}}{E} dt, \quad d\vec{p} = -\Gamma \vec{p} dt + \sqrt{d\tau} \hat{C} \vec{p}$$
  - $\vec{p}$ : Gaussian noise,  $\Gamma$ : drag coefficient,  $\hat{C} = \sqrt{\hat{D}}$  with  $\hat{D}$ : diffusion coefficient
  - use post-point Ito realization of stochastic process [1] with diffusion coefficient  $D_{||} = ET \Rightarrow$  ensures **correct relativistic equilibrium limit**
  - drag and diffusion coefficients: from microscopic models for **elastic HQ scattering**
  - assume D/B-like resonance formation above  $T_c$  [2, 3] or T-matrix approach with **lQCD in-medium qQ potentials** [4]
  - extrapolate cross sections into hadronic phase
- hadronization
  - use coalescence description at decoupling temperature  $T_{dec}$  to recombine c/b quarks with light antiquarks to **D/B mesons**
  - use PYTHIA for semileptonic decay of D/B mesons to “**non-photonic**” electrons
- background medium: UrQMD+hydro model or elliptic-fireball parametrization

## Non-photonic single electrons at RHIC



$R_{AA}$  (left) and  $v_2$  (right) of **non-photonic single electrons** from D- and B-meson decays in  $\sqrt{s_{NN}} = 200$  GeV-Au Au collisions at RHIC, assuming different decoupling temperatures. Using coalescence for hadronization process crucial for consistency between  $R_{AA}$  and  $v_2$  (data from the PHENIX collaboration [5]).

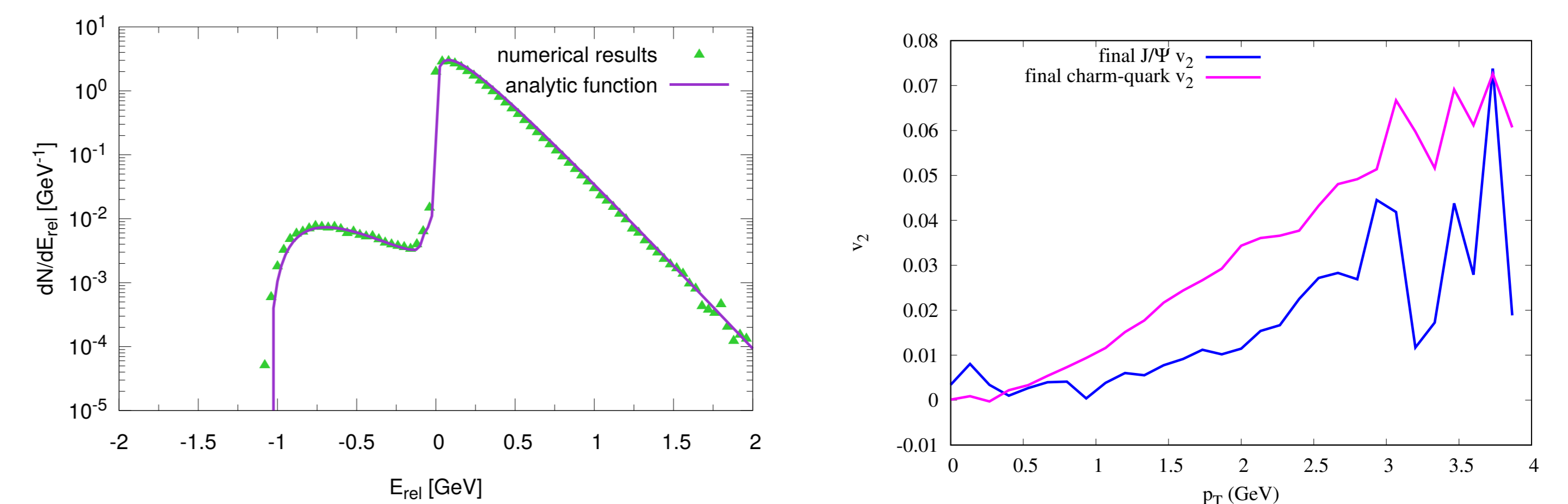
## D-mesons at LHC



$R_{AA}$  (left) and  $v_2$  of **D mesons** in  $\sqrt{s_{NN}} = 2.76$  TeV-Pb Pb collisions at LHC, assuming a decoupling temperature of  $T_{dec} = 130$  MeV (data from the ALICE collaboration [6, 7]).

## Quarkonium-bound states

- Langevin simulation of 1 or several  $c\bar{c}$  pairs [8, 9]
- additional interaction via a  $c\bar{c}$  in-medium UV-regularized screened color-Coulomb potential [10]



**Left:** “Box test”  $c\bar{c}$ -pair-energy distribution in thermal medium with  $T = 160$  MeV; **Right:**  $v_2$  of heavy-quarkonia (“ $J/\Psi$ ”) and c-quarks in semi-central Au+Au collisions at RHIC.

## Conclusions and outlook

- medium modifications of heavy-quark spectra
  - used **UrQMD+hydro** hybrid model for **realistic description of the bulk medium**
  - includes **initial-state fluctuations**
  - heavy c+b-quark diffusion via **Langevin process**
  - elastic resonance scattering of heavy quarks in **strongly interacting matter**
  - coalescence crucial for consistency of  $R_{AA}$  and  $v_2$
  - also used to evaluate dilepton production from **correlated  $D\bar{D}$ -pair decays**
- Quarkonia as classical  $c\bar{c}$ -pair **bound states**
  - additional in-medium  $c\bar{c}$ -potential in Langevin simulation
  - **bound-state formation  $\leftrightarrow$  dissociation** via interaction with medium
- outlook
  - implement **proper quantum description** of bound-state formation
  - possible approaches:
    - in-medium T-matrix
    - Lindhard equation for open quantum systems
    - Schrödinger-Langevin equation
  - also for open-heavy flavor meson formation within the same potential approach!?

## References

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