

# DIPOLE EVOLUTION AND THE PROTON STRUCTURE

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## AT A GLANCE

Space-time structure of MPIs which:

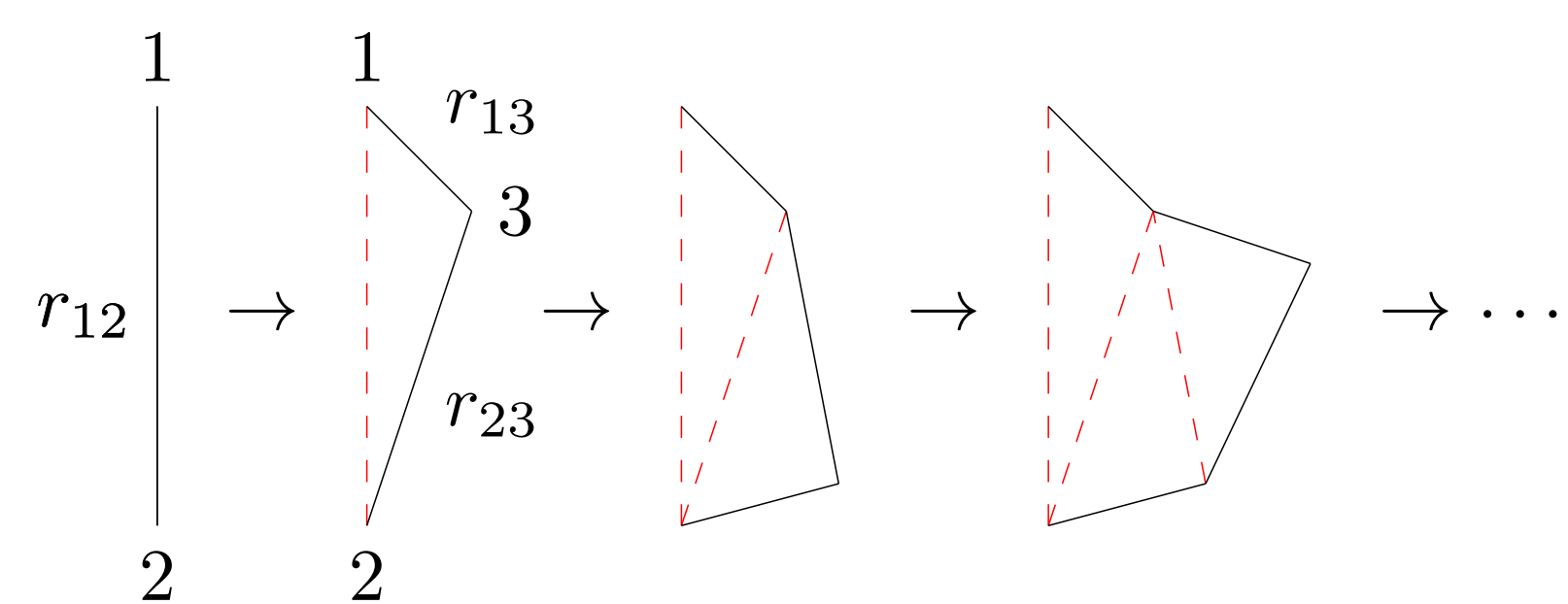
- Predicts eccentricities and normalized symmetric cumulants.
- Is not fitted to flow measurements.
- Is theoretically well motivated.

## DIPOLE EVOLUTION

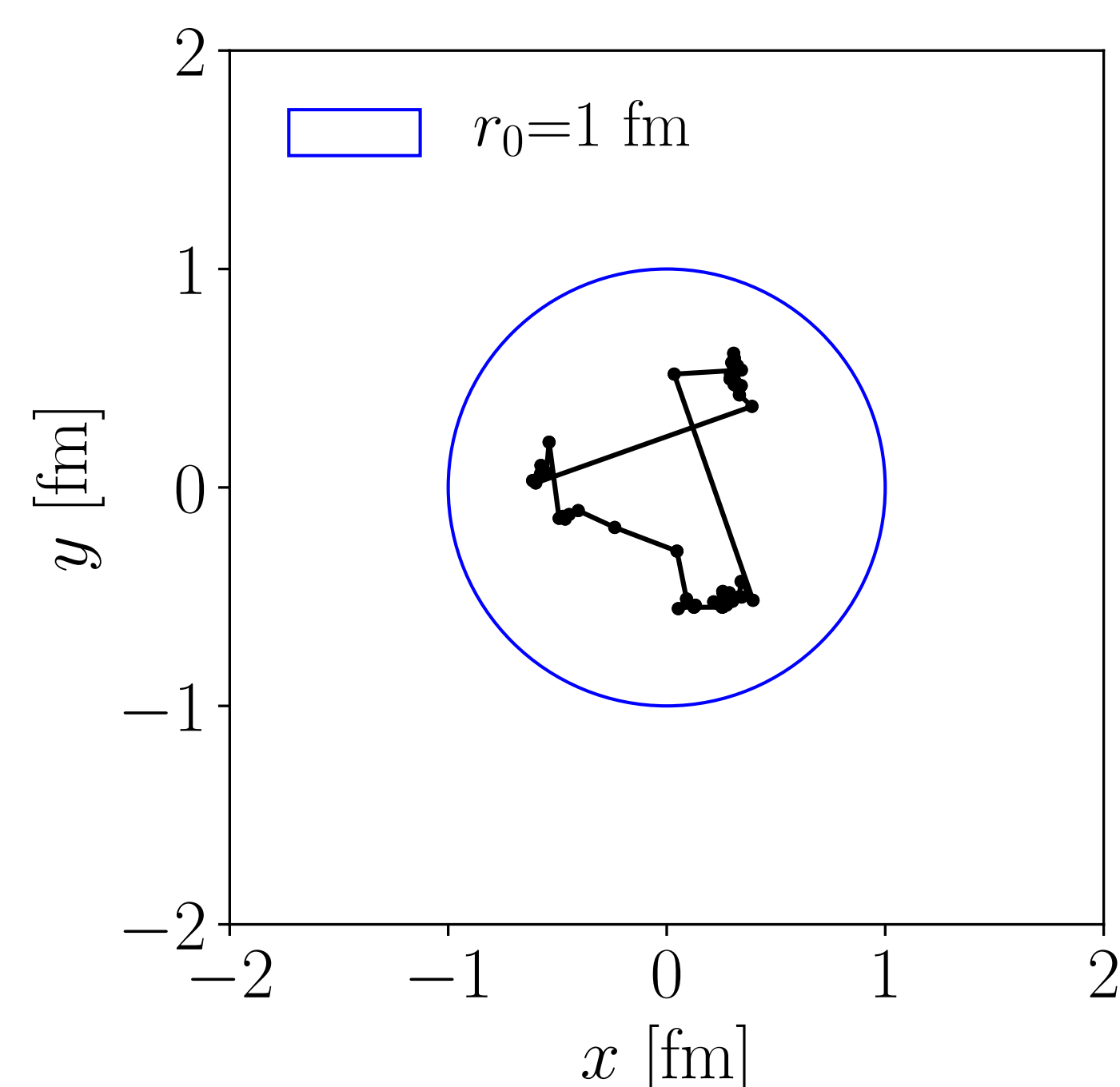
The proton sub-structure is calculated using the Mueller dipole model for QCD. A proton is approximated by three dipoles, evolved in rapidity according to:

$$\frac{d\mathcal{P}}{dy d^2\vec{r}_3} = \frac{N_c \alpha_s}{2\pi^2} \frac{r_{12}^2}{r_{13}^2 r_{23}^2} \Delta(y_{\min}, y),$$

where  $r_{ij}$  denotes transverse sizes as in the sketch, and  $\Delta$  is a Sudakov form factor.

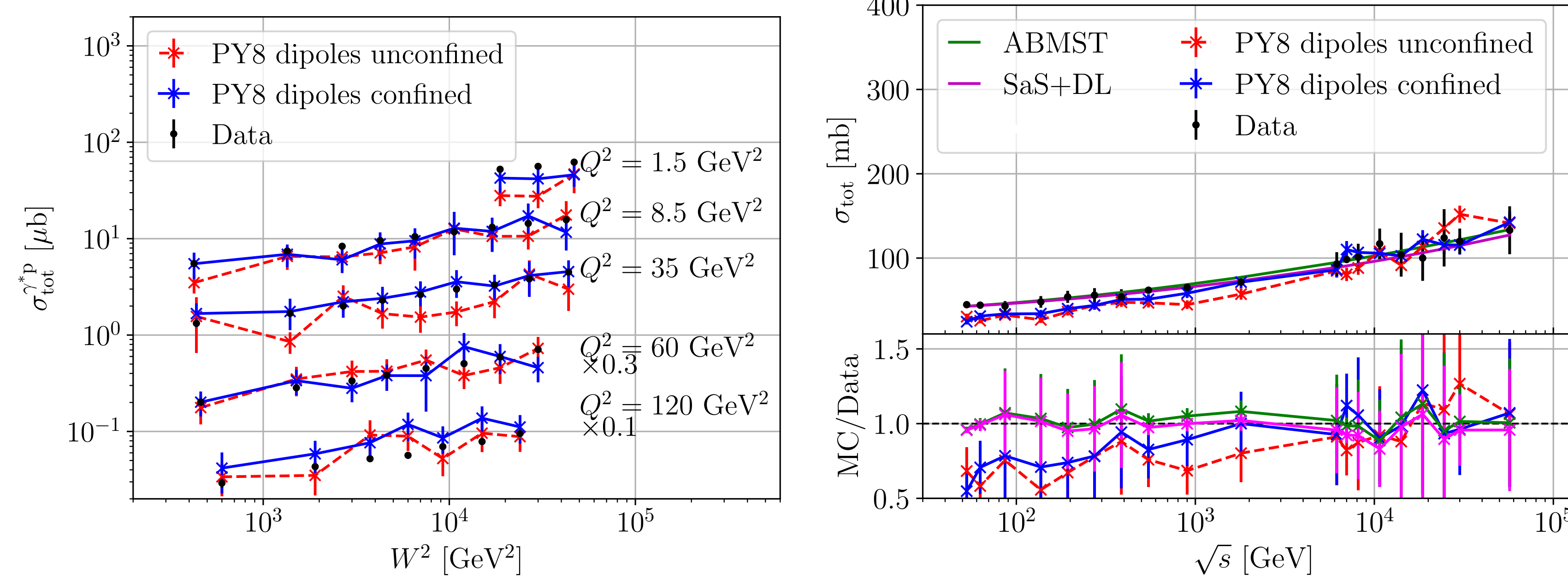


The result is a proton Fock state.

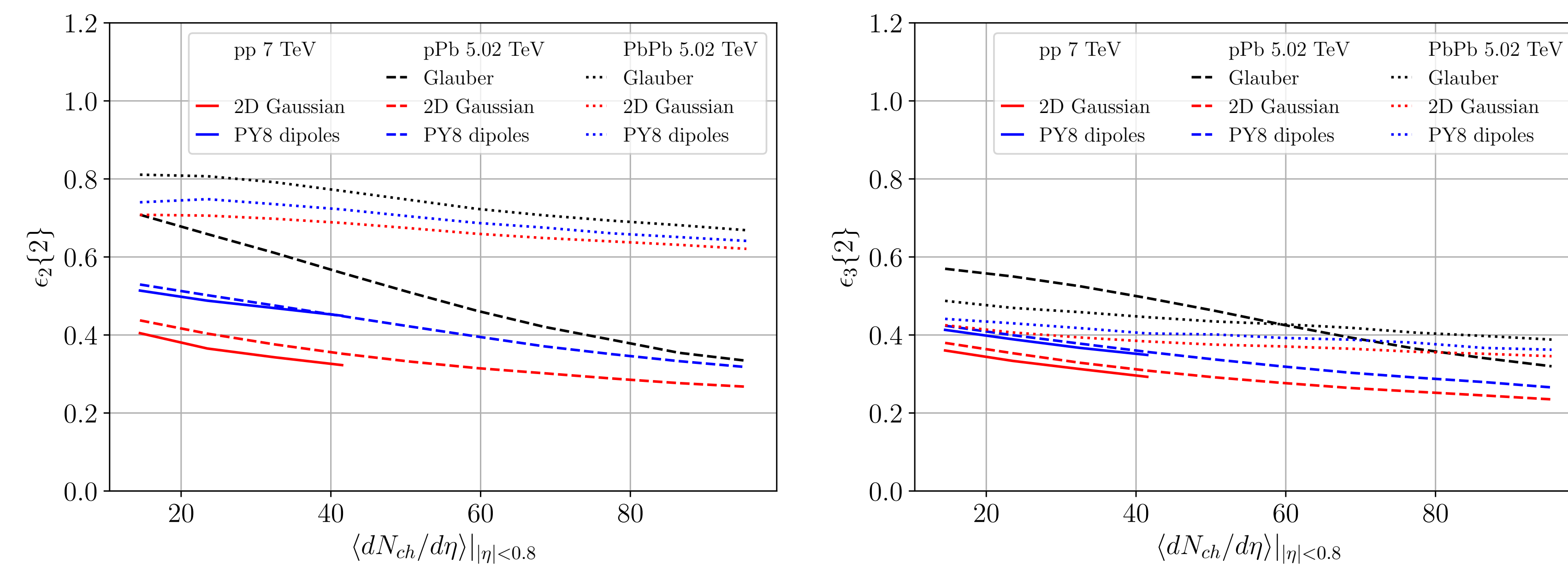


## RESULTS

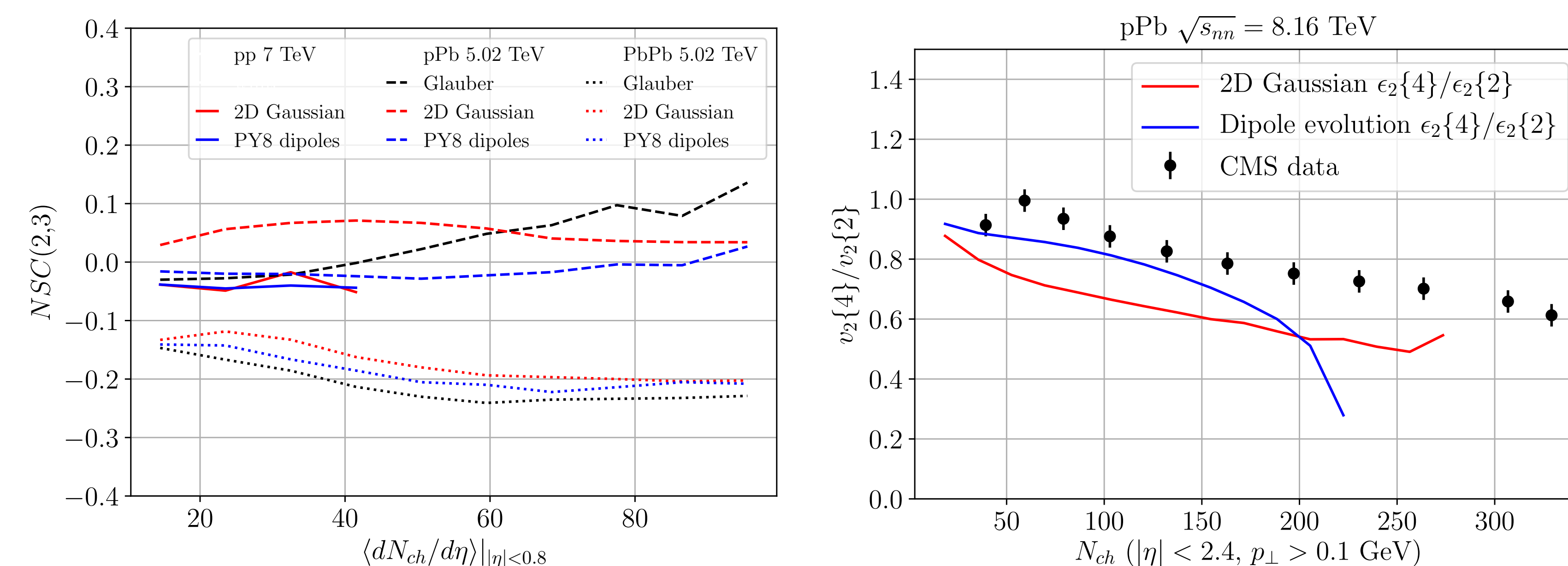
All model parameters are tuned to **ep and pp cross sections**.



**Flow coefficients**  $v_{2,3} \propto \epsilon_{2,3}$  (eccentricities) in a fluid scenario. Peripheral/small systems differentiates between models. Dipole model predicts  $\epsilon_{2,3}$  equal for pp and pPb.



**Normalized symmetric cumulants** and **flow fluctuations** can inform directly about geometry. Best discriminative power in pPb collisions.

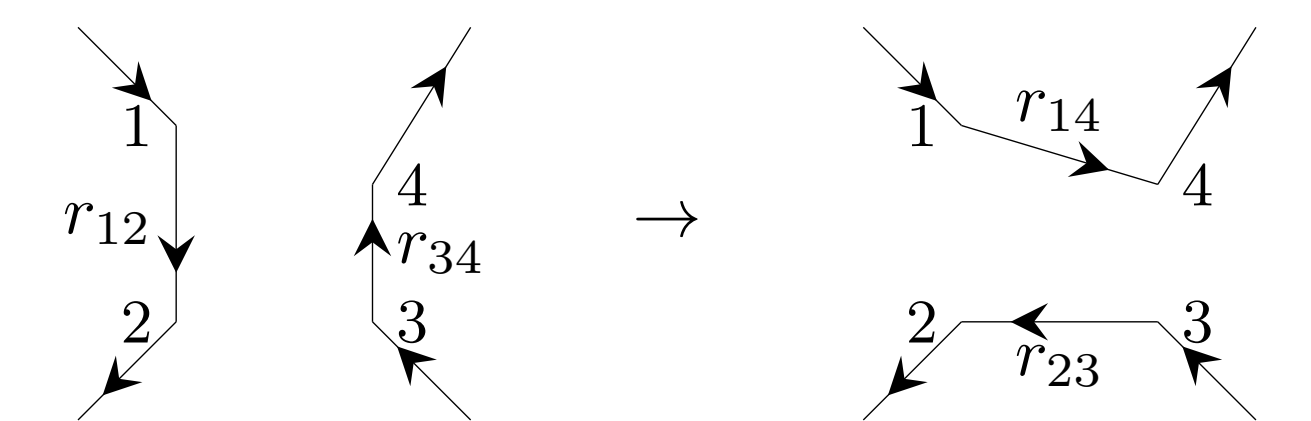


## MATCHING TO MPIs

Pythia MPIs are given a vertex position in transverse space. Either randomly from a 2D-Gaussian, inspired by the proton mass distribution, or according to the dipole evolution. The interaction probability of projectile-target dipole pairs is given at LO by:

$$f_{ij} = \frac{\alpha_s^2}{2} \log^2 \left( \frac{r_{13} r_{24}}{r_{14} r_{23}} \right).$$

where  $r_{ij}$  are distances between dipole ends.



MPIs are placed on dipole interaction vertices with the hardest MPI linked to the most probable interaction.

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Funding from European Research Council (ERC) under the European Union's Horizon 2020 research and innovation program (grant agreement No 668679), the Swedish Research Council, contract numbers 2016-05996 and 2017-0034 as well as the Marie Skłodowska-Curie Innovative Training Network MCnetITN3 (grant agreement 722104) is gratefully acknowledged.

